

COMPLEX NUMBERS. 1

$$i = \sqrt{-1} = i$$

$$\sqrt{-4} = \sqrt{-1 \cdot 4} = \sqrt{-1} \cdot \sqrt{4} = \sqrt{-1} \cdot 2 = 2i$$

$$\sqrt{-36} =$$

$$\sqrt{-64} =$$

$$\sqrt{-2} =$$

$$i^2 = i \cdot i = \sqrt{-1} \cdot \sqrt{-1} = -1$$

$$i^3 =$$

$$i^4 =$$

$$i^5 =$$

$$i^6 =$$

$$i^7 =$$

$$i^8 =$$

Plot on an Argand Diagram: $1 + 2i$, $2 - 3i$, 2

Solve the following equations, indicating the solutions on an Argand Diagram.

1. $x^2 + 4x + 13 = 0$

2. $x^2 + 3x + 2 = 0$

3. $2x^2 + 3x + 5 = 0$

4. $x^2 + 3 = 0$

SUBTRACTION

$$(a + bi) + (c + di) = (a + c) + (b + d)i$$

$$(2 + 3i) + (1 + i) =$$

$$(2 - 3i) + (2 - i) =$$

$$(2 + 5i) - (2 - 3i) =$$

$$(-i) + (4 + i) =$$

AND ON AN ARGAND DIAGRAM

$$(4 + 3i) + (2 + 7i)$$

$$(9 + 5i) - (2 + 3i)$$

$$(9 + 5i) + (-2 - 3i)$$

$$(2 + 3i) + (2 - 3i)$$

$$(2 + 3i) + (2 - 3i)$$

MULTIPLICATION

$$(a + bi) \cdot (c + di) = (ac - bd) + (ad + bc)i$$

$$(2 + 3i)(3 - 5i) =$$

$$(5 + 2i)(4 - 5i) =$$

$$(3 + 4i)(2 - 3i) =$$

$$(4 + 3i)(3 + 4i) =$$

$$(3 + 2i)(3 - 2i) =$$

The Complex Conjugate

$$z = a + bi, \quad \bar{z} = a - bi, \quad z\bar{z} = a^2 + b^2$$

$$z = -3 + 4i, \quad \bar{z} =$$

$$z = 3 - 4i, \quad \bar{z} =$$

$$z = 2i, \quad \bar{z} =$$

$$z = 3, \quad \bar{z} =$$

$$z = 2 + 3i, \quad z\bar{z} =$$

$$z = -3 - 4i, \quad z\bar{z} =$$

$$z = 2, \quad z\bar{z} =$$

$$z = -3i, \quad z\bar{z} =$$

DIVISION

$$\frac{A + Bi}{C} = \frac{A}{C} + \frac{B}{C}i = a + bi$$

$$(a + bi) / (c + di) = \frac{(a + bi)}{(c + di)} = \frac{(a + bi)}{(c + di)} \cdot 1 = \frac{(a + bi)}{(c + di)} \cdot \frac{(c - di)}{(c - di)} = \dots$$

$$\frac{(3 + 2i)}{(4 + 5i)} =$$

EXERCISE

Plot on an Argand Diagram:

$$\frac{(8 + 7i)}{(5 + 2i)}$$

$$\frac{(4 + 9i)}{(2 - 6i)}$$

$$\frac{(3 + 2i)}{(1 - i)} - \frac{(2 + 3i)}{(2 - i)}$$

EXERCISE

The complex impedance Z in a series LCR circuit is given by $Z = R + i\omega L + \frac{1}{i\omega C}$.

Express Z in $a + bi$ form when $R = 10$, $L = 5$, $C = 0.04$ and $\omega = 4$.